Division of space using first Laplacian eigenvalues

$$
\begin{gathered}
\Delta p_{i}+\lambda_{i}^{1} p_{i}=0 \\
\sum_{i} \lambda_{i}^{1}=\text { minimum }
\end{gathered}
$$

We found solution of this problem using the Fleming Viot process Phys.Rev.Lett. 95, 088304 (2005)

## Solution of this minimization problem: based on numerical calculations

In 2D honeycomb lattice


## Solution: based on numerical calculations

> in 3D

3D Weaire-Phelan structure with different volumes of 12-sided and 14 sided polyhedra (with slightly different volumes and curvatures than the Weaire-Phelan structure


